

We claim:

1. A method of determining data flow for a channel having a plurality of subchannels in a multi-carrier system, comprising:
determining data flow for the channel in terms of an input intensity λ_{in} , and a probability of having a frame having no or a correctable number of errors p ; and
adjusting channel performance in accordance with the data flow.

2. The method of claim 1 wherein said data flow is determined in accordance with the following relationships:

$$\begin{aligned}\lambda_{nac} &= \lambda_{in} \frac{[1 - (1 - p)^k] [1 - p]}{p} \\ \lambda_{ti} &= \lambda_{in} \frac{1 - (1 - p)^k}{p}, \\ \lambda_{pout} &= \lambda_{in} [1 - (1 - p)^k], \\ \lambda_{rt} &= \lambda_{in} \frac{(1 - p) [1 - (1 - p)^{k-1}]}{p}, \text{ and} \\ \lambda_{nout} &= \lambda_{in} (1 - p)^k,\end{aligned}$$

λ_{nac} represents a negative acknowledgement intensity, k represents a maximum number of transmissions, λ_{ti} represents a transmitter intensity, λ_{pout} represents an intensity of good and correctable frames; λ_{rt} represents a retransmission intensity; λ_{nout} represents an intensity of erroneous frames that are non-correctable after a maximum number of transmissions.

1 3. The method of claim 2 wherein the data flow is determined by applying said
2 relationships to data flow in a downstream direction, and applying said relationships
3 to data flow in an upstream direction.

1 4. A method of determining data flow for a channel having a plurality of
2 subchannels in a multi-carrier system, comprising:
3 determining an upstream data flow;
4 determining a downstream data flow; and
5 superimposing the upstream data flow and the downstream data flow to
6 determine a channel data flow.

1 5. The method of claim 4 wherein the channel uses forward error correction.

1 6. The method of claim 4 wherein the upstream data flow comprises
2 retransmitting data.

1 7. The method of claim 4 wherein the downstream data flow comprises
2 retransmitting data.

1 8. A method of determining throughput in a multicarrier transmission system having
2 a channel, comprising:
3 generating a representation of the throughput of the channel in a first direction
4 with respect to the throughput of the channel in a second direction; and
5 determining the throughput of the channel in a first direction with respect to
6 the throughput of the channel in a second direction using the representation.

9. The method of claim 8 wherein the representation is generated in accordance with the following relationships:

$$\frac{M_d}{K_d} \left[\frac{1}{m_d} + \frac{1-p_d}{p_d} \right] [1 - (1-p_d)^{k_d}] \Lambda_d + \frac{N_u}{K_u} \frac{1 - (1-p_u)^{k_u}}{p_u} \Lambda_u \leq V_u, \text{ and}$$
$$\frac{N_d}{K_d} \frac{1 - (1-p_d)^{k_d}}{p_d} \Lambda_d + \frac{M_u}{K_u} \left[\frac{1}{m_u} + \frac{1-p_u}{p_u} \right] [1 - (1-p_u)^{k_u}] \Lambda_u \leq V_d,$$

wherein M_d represents a length of an acknowledgment frame in a downstream direction, K_d represents the length of an information field in the downstream direction, m_d represents a number of information frames between positive acknowledgment frames in the downstream direction, p_d represents a probability of an information frame being accepted in the downstream direction, k_d represents a maximum number of transmissions in the downstream direction, Λ_d represents a number of information bits per unit time in the downstream direction, N_d represents a total frame length in the downstream direction, M_u represents a length of an acknowledgment frame in an upstream direction, N_u represents a total frame length in the upstream direction, K_u represents the length of an information field in the upstream direction, m_u represents a number of information frames between positive acknowledgment frames in the upstream direction, p_u represents a probability of an information frame being accepted in the upstream direction, k_u represents a maximum number of transmissions in the upstream direction, Λ_u represents a number of information bits per unit time in the upstream direction, V_u represents a data rate in the upstream direction, and V_d represents a data rate in the downstream direction.

10. A method of determining throughput in a multicarrier transmission system,
comprising:
determining the throughput of a channel in an upstream and downstream direction
in accordance with the following relationships:

$$H_u = \max \Lambda_u = \min \left\{ \begin{aligned} &V_u / \left[\frac{N_d}{K_d} \frac{1 - (1 - p_d)^{k_d}}{p_d} + \frac{M_u}{K_u} \frac{V_u}{V_d} \left(\frac{1}{m_u} + \frac{1 - p_u}{p_u} \right) (1 - (1 - p_u)^{k_u}) \right], \\ &V_u / \left[\frac{M_d}{K_d} \frac{V_d}{V_u} \left(\frac{1}{m_d} + \frac{1 - p_d}{p_d} \right) (1 - (1 - p_d)^{k_d}) + \frac{N_u}{K_u} \frac{1 - (1 - p_u)^{k_u}}{p_u} \right] \end{aligned} \right\}, \text{ and}$$
$$H_d = \max \Lambda_d = \min \left\{ \begin{aligned} &V_d / \left[\frac{N_d}{K_d} \frac{1 - (1 - p_d)^{k_d}}{p_d} + \frac{M_u}{K_u} \frac{V_u}{V_d} \left(\frac{1}{m_u} + \frac{1 - p_u}{p_u} \right) (1 - (1 - p_u)^{k_u}) \right], \\ &V_d / \left[\frac{M_d}{K_d} \frac{V_d}{V_u} \left(\frac{1}{m_d} + \frac{1 - p_d}{p_d} \right) (1 - (1 - p_d)^{k_d}) + \frac{N_u}{K_u} \frac{1 - (1 - p_u)^{k_u}}{p_u} \right] \end{aligned} \right\},$$

wherein M_d represents a length of an acknowledgment frame in a downstream direction, K_d represents the length of an information field in the downstream direction, m_d represents a number of information frames between positive acknowledgment frames in the downstream direction, p_d represents a probability of an information frame being accepted in the downstream direction, k_d represents a maximum number of transmissions in the downstream direction, Λ_d represents a number of information bits per unit time in the downstream direction, N_d represents a total frame length in the downstream direction, M_u represents a length of an acknowledgment frame in an upstream direction, N_u represents a total frame length in the upstream direction, K_u represents the length of an information field in the upstream direction, m_u represents a number of information frames between positive acknowledgment frames in the upstream direction, p_u represents a probability of an information frame being accepted in the upstream direction, k_u represents a maximum number of transmissions in the upstream direction, Λ_u represents a number of

23 information bits per unit time in the upstream direction, V_u represents a data rate in
24 the upstream direction, and V_d represents a data rate in the downstream direction.

1 11. A method of increasing a bit load of a multicarrier system comprising a channel
2 having a plurality of subchannels, comprising:

3 determining a bit load for at least one subchannel based on a target symbol error
4 rate ϵ_s , a maximum number of symbol errors that can be corrected t , a number of symbols
5 in an information field K , and a maximum number of transmissions k , and a number of
6 bits per subchannel; and

7 selecting the maximum number of symbol errors t , the number of symbols in
8 the information field K and the maximum number of transmissions k , such that a
9 coding gain is increased.

1 12. The method of claim 11 wherein the coding gain is a function of an average
2 number of transmissions for a frame.

1 13. The method of claim 11 wherein the bit load is determined in accordance with the
2 following relationships:
3

4

$$1 - \left(1 - W(t, K, k) \epsilon_s^{\frac{1}{(t+1)k}} \right)^{1/\alpha}$$
$$= \omega(b_i) (1 - 2^{-b_i/2}) \operatorname{erfc} \left(\sqrt{3 \cdot 10^{\gamma_i/10} / (2^{b_i+1} - 2)} \right) \left[2 - (1 - 2^{-b_i/2}) \operatorname{erfc} \left(\sqrt{3 \cdot 10^{\gamma_i/10} / (2^{b_i+1} - 2)} \right) \right]$$

5

6 wherein b_i represents a number of bits per subchannel, γ_i represents a signal-to-noise ratio
7 at the i -th subchannel, $\omega(b_i)$ represents an average fraction of erroneous bits in a b_i -sized
8 erroneous quadrature-amplitude-modulation symbol, ϵ_s represents a target symbol error
9 rate, β represents an effect of a descrambler, and α represent a number of bits per code
10 symbol; and

$$W(t, K, k) = \left[\binom{K+C+R-1}{t} \right]^{\frac{1}{(t+1)k}} \left[\binom{K+C+R}{t+1} \right]^{\frac{k-1}{(t+1)k}}$$

C+R represents a number of redundant symbols in an error correction field, and the net coding gain $G_n(t, K, k)$ is determined in accordance with the following relationship:

$$G_n(t, K, k) \equiv \frac{K}{K+C+R} \frac{B_{DMT}(t, K, k)}{\nu} - \frac{K}{K+C} B_{DMT}(0, K, 1)$$

ν represents an average number of transmissions, and $B_{DMT}(t, K, k)$ represents a number of bits in a discrete multitone symbol based on the values of t , K and k .

14. The method of claim 13 wherein $\omega(b_i)$ is approximated in accordance with the following relationship:

$$\omega(b_i) = \frac{4}{3 + 2b_i}$$

15. The method of claim 13 wherein ε_s is determined in accordance with the following relationship:

$$\varepsilon_s = 1 - \left(1 - \frac{\varepsilon}{\beta} \right)^\alpha,$$

and ε represents a target bit error rate, α represents a length of a code symbol, and β represents the effect of a descrambler.

1 16. The method of claim 13 wherein $\omega(b_i)$ is determined in accordance with the
2 following relationship:

3

$$4 \quad \omega(b) = \frac{1}{b \cdot 2^b} \sum_{i=1}^{2^b} \sum_{j \neq i}^{\chi_i} \frac{d_H(a_i, a_j)}{\chi_i},$$

5

6 b represents a number of bit positions of a quadrature-amplitude-modulation symbol,
7 a_i represents a label for the i^{th} point of a constellation associated with a subchannel, a_j
8 represents a label for the j^{th} point of a constellation associated with a subchannel, and
9 χ_i represents a coordination number of the a_i^{th} point, $d_H(a_i, a_j)$ represents a Hamming
10 distance between respective binary vectors associated with points a_i and a_j .

1 17. The method of claim 11 further comprising:
2 determining a total increase in the number of bits to be sent in a DMT symbol
3 ($G_l(t, K, k)$) in accordance with the following relationship:

4

$$5 \quad G_d(t, K, k) \equiv B_{DMT}(t, K, k) - B_{DMT}(0, K, 1).$$

1 18. A method of determining an uncoded bit error rate p_b based on a target symbol
2 error rate ε_s and a maximum number of transmissions k , comprising:

3 determining the uncoded bit error rate p_b based on a weighted series expansion of
4 the target bit error rate ε_s , comprising weights W that are a function of a maximum
5 number of symbol errors that can be corrected t and a number of symbols in an
6 information field K ; and

7 selecting the maximum number of symbol errors t , the number of symbols in the
8 information field K and the maximum number of transmissions k , such that the uncoded
9 bit error rate p_b that produces a symbol error rate that is less than or equal to the target
10 symbol error rate ε_s is largest.

19. The method of claim 18 wherein said weighted series expansion to determine said uncoded bit error rate p_b comprises the following relationship:

$$p_b = 1 - \left(1 - W(t, K, k) \varepsilon_s^{\frac{1}{(t+1)k}} \right)^{1/\alpha}$$

wherein

$$W(t, K, k) = \left[\binom{K+C+R-1}{t} \right]^{\frac{1}{(t+1)k}} \left[\binom{K+C+R}{t+1} \right]^{\frac{k-1}{(t+1)k}},$$

C+R represents a number of redundant symbols in an error correction field.

20. A method of selecting transmission parameters a multicarrier system having a channel comprising a plurality of subchannels, comprising:

selecting a number (s) of discrete multi-tone symbols in a forward-error-correction frame, a number (z) of forward-error-correction control symbols in a discrete multitone symbol, and a maximum number of transmissions (k), based on a signal-to-noise ratio and a number of subchannels associated with the signal-to-noise ratio; and

transmitting information in accordance with the selected number (s) of discrete multi-tone symbols, the number (z) of forward-error-correction control symbols in the discrete multitone symbol and the maximum number of transmissions (k).

1 21. The method of claim 20 wherein said selecting comprises selecting an
2 adjustment value per subchannel based on the signal-to-noise ratio and the number of
3 subchannels associated with the signal-to-noise ratio; and
4 adjusting a number of bits per subchannel for at least one subchannel in
5 accordance with the adjustment value.

1 22. The method of claim 20 wherein the signal-to-noise ratio is an average
2 signal-to-noise ratio of the associated number of subchannels.

1 23. The method of claim 20 further comprising:
2 storing, in a table, the number (s) of discrete multi-tone symbols in the
3 forward-error-correction frame, the number (z) of forward-error-correction control
4 symbols in the discrete multitone symbol associated with the signal-to-noise ratio, the
5 maximum number of transmissions (k) and the number of subchannels associated
6 with the signal-to-noise ratio, for different values of s, z, signal-to-noise ratios and
7 numbers of subchannels.

1 24. The method of claim 23 wherein for each value of signal-to-noise ratio and
2 number of bits per subchannel of the table, the associated values of s, z and k are also
3 associated with an adjustment value that provides a maximal net coding gain g_n , such
4 that the associated values of s, z and k is selected from a subset of associated s, z and
5 k values.

1 25. A method of determining an optimum bit load b per subchannel in a multicarrier
2 system with forward error correction, comprising:
3 computing one or more values of a maximum number of symbol errors that
4 can be corrected t, a number of symbols in the information field K and a maximum

number of transmissions k to determine the optimum bit load per subchannel in accordance with the following relationship:

$$b = [\gamma + \Phi(\gamma, t, K, k, \varepsilon)] / 10 \log 2$$

wherein

$$\Phi(\gamma, t, K, k, \varepsilon) = 10 \log \left\{ 10^{-\gamma/10} + \frac{3 \log e}{2 \log \left[\frac{\alpha \langle \omega(b) \rangle \sqrt{8/\pi}}{W(t, K, k) (\alpha \varepsilon / \beta)^{\frac{1}{(t+1)k}}} \right] - \log \log \left[\frac{\alpha \langle \omega(b) \rangle \sqrt{8/\pi}}{W(t, K, k) (\alpha \varepsilon / \beta)^{\frac{1}{(t+1)k}}} \right] + \log \left(\frac{\log e}{2} \right)} \right\}$$

$$W(t, K, k) = \left[\binom{K+C+R-1}{t} \right]^{\frac{1}{(t+1)k}} \left[\binom{K+C+R}{t+1} \right]^{\frac{k-1}{(t+1)k}},$$

$$\langle \omega(b) \rangle = \frac{1}{b_{\max}} \int_1^{b_{\max}} \omega(b) (1 - 2^{-b/2}) db$$

α represents a number of bits per symbol, γ represents a signal-to-noise ratio, ε represents a target symbol error rate, k represents a maximum number of transmissions, $C+R$ represents a number of redundant symbols in an error correction field, b represents a number of bit positions of a quadrature-amplitude-modulation symbol, $\omega(b)$ represents an average fraction of erroneous bits in an erroneous b -sized quadrature-amplitude-modulation symbol, and b_{\max} is a maximum number of bit positions of the quadrature-amplitude-modulation symbol per subchannel; and selecting a bit load per subchannel in accordance with the maximum number of symbol errors that can be corrected t , a number of symbols in the information field K and the maximum number of transmissions k .

1 26. A method for transmitting data in a multi-carrier system between a
2 downstream station and an upstream station, coupled by a channel having a plurality
3 of subchannels, comprising:

4 transmitting an information frame from the upstream station;
5 receiving the information frame at the downstream station;
6 determining whether the information frame is non-correctable;
7 transmitting a negative acknowledgement when the information frame is
8 non-correctable; and

9 transmitting the information frame if the information frame has not be
10 transmitted a predetermined number of times from the upstream station.

1 27. The method of claim 26 wherein the predetermined number of times is
2 determined in accordance with a measured signal-to-noise ratio value representing at
3 least a subset of the subchannels of the channel, and forward error correction
4 parameters.

1 28. The method of claim 26 wherein the multi-carrier system is a discrete
2 multi-tone system.

1 29. The method of claim 26 wherein the discrete multi-tone system comprises the
2 G-lite standard.

1 30. The method of claim 26 wherein the discrete multi-tone system comprises the
2 G.dmt standard.

1 31. The method of claim 26 wherein the forward error correction parameters are
2 Reed-Solomon forward error correction parameters.

32. An apparatus for determining throughput in a multicarrier transmission system having a channel, comprising:
means for generating a representation of the throughput of the channel in a first direction with respect to the throughput of the channel in a second direction; and
means for determining the throughput of the channel in a first direction with respect to the throughput of the channel in a second direction using the representation.

33. The apparatus of claim 32 wherein the representation is generated in accordance with the following relationships:

$$\frac{M_d}{K_d} \left[\frac{1}{m_d} + \frac{1-p_d}{p_d} \right] [1 - (1-p_d)^{k_d}] \Lambda_d + \frac{N_u}{K_u} \frac{1 - (1-p_u)^{k_u}}{p_u} \Lambda_u \leq V_u, \text{ and}$$

$$\frac{N_d}{K_d} \frac{1 - (1-p_d)^{k_d}}{p_d} \Lambda_d + \frac{M_u}{K_u} \left[\frac{1}{m_u} + \frac{1-p_u}{p_u} \right] [1 - (1-p_u)^{k_u}] \Lambda_u \leq V_d,$$

wherein M_d represents a length of an acknowledgment frame in a downstream direction, K_d represents the length of an information field in the downstream direction, m_d represents a number of information frames between positive acknowledgment frames in the downstream direction, p_d represents a probability of an information frame being accepted in the downstream direction, k_d represents a maximum number of transmissions in the downstream direction, Λ_d represents a number of information bits per unit time in the downstream direction, N_d represents a total frame length in the downstream direction, M_u represents a length of an acknowledgment frame in an upstream direction, N_u represents a total frame length in the upstream direction, K_u represents the length of an information field in the upstream direction, m_u represents a number of information frames between positive acknowledgment frames in the upstream direction, p_u represents a probability of an information frame being accepted in the upstream direction, k_u

20 represents a maximum number of transmissions in the upstream direction, Λ_u represents a
 21 number of information bits per unit time in the upstream direction, V_u represents a data
 22 rate in the upstream direction, and V_d represents a data rate in the downstream direction.

34. An apparatus for determining throughput in a multicarrier transmission system,
 comprising:

means for determining the throughput of a channel in an upstream and
 downstream direction in accordance with the following relationships:

$$H_u = \max \Lambda_u = \min \left\{ \begin{array}{l} V_u / \left[\frac{N_d}{K_d} \frac{1 - (1 - p_d)^{k_d}}{p_d} + \frac{M_u}{K_u} \frac{V_u}{V_d} \left(\frac{1}{m_u} + \frac{1 - p_u}{p_u} \right) (1 - (1 - p_u)^{k_u}) \right], \\ V_u / \left[\frac{M_d}{K_d} \frac{V_d}{V_u} \left(\frac{1}{m_d} + \frac{1 - p_d}{p_d} \right) (1 - (1 - p_d)^{k_d}) + \frac{N_u}{K_u} \frac{1 - (1 - p_u)^{k_u}}{p_u} \right] \end{array} \right\}, \text{ and}$$

$$H_d = \max \Lambda_d = \min \left\{ \begin{array}{l} V_d / \left[\frac{N_d}{K_d} \frac{1 - (1 - p_d)^{k_d}}{p_d} + \frac{M_u}{K_u} \frac{V_u}{V_d} \left(\frac{1}{m_u} + \frac{1 - p_u}{p_u} \right) (1 - (1 - p_u)^{k_u}) \right], \\ V_d / \left[\frac{M_d}{K_d} \frac{V_d}{V_u} \left(\frac{1}{m_d} + \frac{1 - p_d}{p_d} \right) (1 - (1 - p_d)^{k_d}) + \frac{N_u}{K_u} \frac{1 - (1 - p_u)^{k_u}}{p_u} \right] \end{array} \right\},$$

wherein M_d represents a length of an acknowledgment frame in a downstream direction,
 K_d represents the length of an information field in the downstream direction, m_d
 represents a number of information frames between positive acknowledgment frames in
 the downstream direction, p_d represents a probability of an information frame being
 accepted in the downstream direction, k_d represents a maximum number of transmissions
 in the downstream direction, Λ_d represents a number of information bits per unit time in
 the downstream direction, N_d represents a total frame length in the downstream direction,
 M_u represents a length of an acknowledgment frame in an upstream direction, N_u
 represents a total frame length in the upstream direction, K_u represents the length of an

19 information field in the upstream direction, m_u represents a number of information frames
20 between positive acknowledgment frames in the upstream direction, p_u represents a
21 probability of an information frame being accepted in the upstream direction, k_u
22 represents a maximum number of transmissions in the upstream direction, Λ_u represents a
23 number of information bits per unit time in the upstream direction, V_u represents a data
24 rate in the upstream direction, and V_d represents a data rate in the downstream direction.

1 35. An apparatus for increasing a bit load of a multicarrier system comprising a
2 channel having a plurality of subchannels, comprising:

3 means for determining a bit load for at least one subchannel based on a target
4 symbol error rate \mathcal{E}_s , a maximum number of symbol errors that can be corrected t , a
5 number of symbols in an information field K , and a maximum number of transmissions k ,
6 and a number of bits per subchannel; and

7 means for selecting the maximum number of symbol errors t , the number of
8 symbols in the information field K and the maximum number of transmissions k , such
9 that a coding gain is increased.

1 36. The apparatus of claim 35 wherein the coding gain is a function of an average
2 number of transmissions for a frame.

1 37. The apparatus of claim 35 wherein the bit load is determined in accordance with
2 the following relationships:

3

$$1 - \left(1 - W(t, K, k) \mathcal{E}_s^{\frac{1}{(t+1)k}} \right)^{1/\alpha}$$

4

$$= \omega(b_i) (1 - 2^{-b_i/2}) \operatorname{erfc} \left(\sqrt{3 \cdot 10^{\gamma_i/10} / (2^{b_i+1} - 2)} \right) \left[2 - (1 - 2^{-b_i/2}) \operatorname{erfc} \left(\sqrt{3 \cdot 10^{\gamma_i/10} / (2^{b_i+1} - 2)} \right) \right]$$

5

wherein b_i represents a number of bits per subchannel, γ_i represents a signal-to-noise ratio at the i -th subchannel, $\omega(b_i)$ represents an average fraction of erroneous bits in a b_i -sized erroneous quadrature-amplitude-modulation symbol, ε_s represents a target symbol error rate, β represents an effect of a descrambler, and α represent a number of bits per code symbol; and

$$W(t, K, k) = \left[\binom{K+C+R-1}{t} \right]^{-\frac{1}{(t+1)k}} \left[\binom{K+C+R}{t+1} \right]^{-\frac{k-1}{(t+1)k}}$$

$C+R$ represents a number of redundant symbols in an error correction field, and the net coding gain $G_n(t, K, k)$ is determined in accordance with the following relationship:

$$G_n(t, K, k) \equiv \frac{K}{K+C+R} \frac{B_{DMT}(t, K, k)}{\nu} - \frac{K}{K+C} B_{DMT}(0, K, 1)$$

ν represents an average number of transmissions, and $B_{DMT}(t, K, k)$ represents a number of bits in a discrete multitone symbol based on the values of t , K and k .

38. The apparatus of claim 37 wherein $\omega(b_i)$ is approximated in accordance with the following relationship:

$$\omega(b_i) = \frac{4}{3 + 2b_i}$$

39. The apparatus of claim 37 wherein ε_s is determined in accordance with the following relationship:

$$\varepsilon_s = 1 - \left(1 - \frac{\varepsilon}{\beta} \right)^\alpha,$$

and ε represents a target bit error rate, α represents a length of a code symbol, and β represents the effect of a descrambler.

40. The apparatus of claim 37 wherein $\omega(b_i)$ is determined in accordance with the following relationship:

$$\omega(b) = \frac{1}{b \cdot 2^b} \sum_{i=1}^{2^b} \sum_{j \neq i}^{\chi_i} \frac{d_H(a_i, a_j)}{\chi_i},$$

b represents a number of bit positions of a quadrature-amplitude-modulation symbol, a_i represents a label for the i^{th} point of a constellation associated with a subchannel, a_j represents a label for the j^{th} point of a constellation associated with a subchannel, and χ_i represents a coordination number of the a_i^{th} point, $d_H(a_i, a_j)$ represents a Hamming distance between respective binary vectors associated with points a_i and a_j .

41. The apparatus of claim 35 further comprising:

means for determining a total increase in the number of bits to be sent in a DMT symbol ($G_i(t, K, k)$) in accordance with the following relationship:

$$G_d(t, K, k) \equiv B_{DMT}(t, K, k) - B_{DMT}(0, K, 1) \quad .$$

42. An apparatus for determining an uncoded bit error rate p_b based on a target symbol error rate ϵ_s and a maximum number of transmissions k , comprising:

means for determining the uncoded bit error rate p_b based on a weighted series expansion of the target bit error rate ϵ_s , comprising weights W that are a function of a maximum number of symbol errors that can be corrected t and a number of symbols in an information field K ; and

means for selecting the maximum number of symbol errors t , the number of symbols in the information field K and the maximum number of transmissions k , such that the uncoded bit error rate p_b that produces a symbol error rate that is less than or equal to the target symbol error rate ϵ_s is largest.

43. The apparatus of claim 42 wherein said weighted series expansion to determine said uncoded bit error rate p_b comprises the following relationship:

$$p_b = 1 - \left(1 - W(t, K, k) \epsilon_s^{\frac{1}{(t+1)k}} \right)^{1/\alpha}$$

wherein

$$W(t, K, k) = \left[\binom{K+C+R-1}{t} \right]^{-\frac{1}{(t+1)k}} \left[\binom{K+C+R}{t+1} \right]^{-\frac{k-1}{(t+1)k}},$$

$C+R$ represents a number of redundant symbols in an error correction field.

1 44. An apparatus for selecting transmission parameters a multicarrier system
2 having a channel comprising a plurality of subchannels, comprising:
3 means for selecting a number (s) of discrete multi-tone symbols in a
4 forward-error-correction frame, a number (z) of forward-error-correction control
5 symbols in a discrete multitone symbol, and a maximum number of transmissions (k),
6 based on a signal-to-noise ratio and a number of subchannels associated with the
7 signal-to-noise ratio; and
8 means for transmitting information in accordance with the selected number (s)
9 of discrete multi-tone symbols, the number (z) of forward-error-correction control
10 symbols in the discrete multitone symbol and the maximum number of transmissions
11 (k).

1 45. The apparatus of claim 44 wherein said means for selecting comprises
2 selecting an adjustment value per subchannel based on the signal-to-noise ratio and
3 the number of subchannels associated with the signal-to-noise ratio; and
4 means for adjusting a number of bits per subchannel for at least one
5 subchannel in accordance with the adjustment value.

1 46. The apparatus of claim 44 wherein the signal-to-noise ratio is an average
2 signal-to-noise ratio of the associated number of subchannels.

1 47. The apparatus of claim 44 further comprising:
2 means for storing, in a table, the number (s) of discrete multi-tone symbols in
3 the forward-error-correction frame, the number (z) of forward-error-correction
4 control symbols in the discrete multitone symbol associated with the signal-to-noise
5 ratio, the maximum number of transmissions (k) and the number of subchannels
6 associated with the signal-to-noise ratio, for different values of s, z, signal-to-noise
7 ratios and numbers of subchannels.

48. The apparatus of claim 47 wherein for each value of signal-to-noise ratio and number of bits per subchannel of the table, the associated values of s , z and k are also associated with an adjustment value that provides a maximal net coding gain g_n , such that the associated values of s , z and k is selected from a subset of associated s , z and k values.

49. An apparatus for determining an optimum bit load b per subchannel in a multicarrier system with forward error correction, comprising:
means for computing one or more values of a maximum number of symbol errors that can be corrected t , a number of symbols in the information field K and a maximum number of transmissions k to determine the optimum bit load per subchannel in accordance with the following relationship:

$$b = [\gamma + \Phi(\gamma, t, K, k, \epsilon)] / 10 \log 2$$

wherein

$$\Phi(\gamma, t, K, k, \epsilon) = 10 \log \left\{ 10^{-\gamma/10} + \frac{3 \log e}{2 \log \left[\frac{\alpha \langle \omega(b) \rangle \sqrt{8/\pi}}{W(t, K, k) (\alpha \epsilon / \beta)^{\frac{1}{(t+1)k}}} \right] - \log \log \left[\frac{\alpha \langle \omega(b) \rangle \sqrt{8/\pi}}{W(t, K, k) (\alpha \epsilon / \beta)^{\frac{1}{(t+1)k}}} \right] + \log \left(\frac{\log e}{2} \right)} \right\}$$

$$W(t, K, k) = \left[\binom{K+C+R-1}{t} \right]^{\frac{1}{(t+1)k}} \left[\binom{K+C+R}{t+1} \right]^{\frac{k-1}{(t+1)k}},$$

$$\langle \omega(b) \rangle = \frac{1}{b_{\max}} \int_1^{b_{\max}} \omega(b) (1 - 2^{-b/2}) db$$

18 α represents a number of bits per symbol, γ represents a signal-to-noise ratio, ϵ
19 represents a target symbol error rate, k represents a maximum number of
20 transmissions, $C+R$ represents a number of redundant symbols in an error correction
21 field, b represents a number of bit positions of a quadrature-amplitude-modulation
22 symbol, $\omega(b)$ represents an average fraction of erroneous bits in an erroneous b -sized
23 quadrature-amplitude-modulation symbol, and b_{max} is a maximum number of bit
24 positions of the quadrature-amplitude-modulation symbol per subchannel; and
25 means for selecting a bit load per subchannel in accordance with the
26 maximum number of symbol errors that can be corrected t , a number of symbols in
27 the information field K and the maximum number of transmissions k .

1 50. A method for transmitting data in a multi-carrier system between a
2 downstream station and an upstream station, coupled by a channel having a plurality
3 of subchannels, comprising:
4 a transmitter to transmit an information frame from the upstream station;
5 a receiver to receive the information frame at the downstream station, the
6 receiver to determine whether the information frame is non-correctable, and transmit
7 a negative acknowledgement when the information frame is non-correctable;
8 wherein the transmitter, in response to the negative acknowledgment,
9 transmits the information frame if the information frame has not be transmitted a
10 predetermined number of times from the upstream station.

1 51. The apparatus of claim 50 wherein the predetermined number of times is
2 determined in accordance with a measured signal-to-noise ratio value representing at
3 least a subset of the subchannels of the channel, and forward error correction
4 parameters.

1 52. The apparatus of claim 50 wherein the multi-carrier system is a discrete
2 multi-tone system.

1 53. The apparatus of claim 50 wherein the discrete multi-tone system comprises
2 the G-lite standard.

1 54. The apparatus of claim 50 wherein the discrete multi-tone system comprises
2 the G.dmt standard.

1 55. The apparatus of claim 50 wherein the forward error correction parameters are
2 Reed-Solomon forward error correction parameters.

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